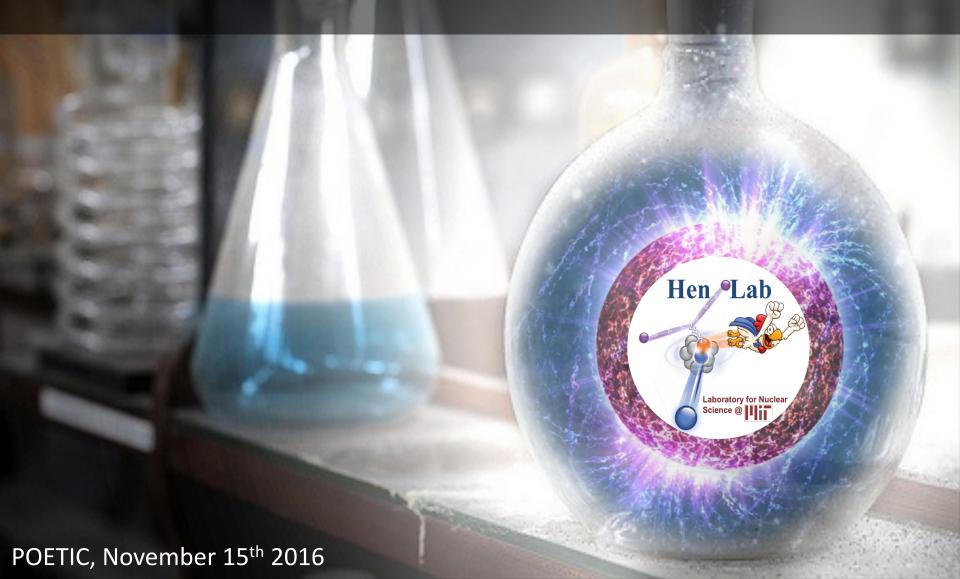
Short-Range Nuclear Structure Or Hen – MIT





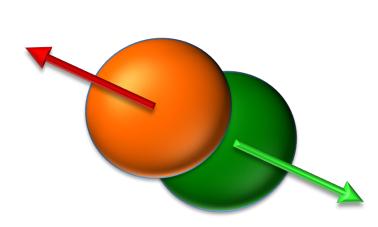
SRC 101



SRC are pairs of nucleon that are close together in the nucleus (wave functions overlap)

=> Momentum space: pairs with <u>high relative</u> <u>momentum</u> and <u>low c.m. momentum</u> compared to the

Fermi momentum (k_F)



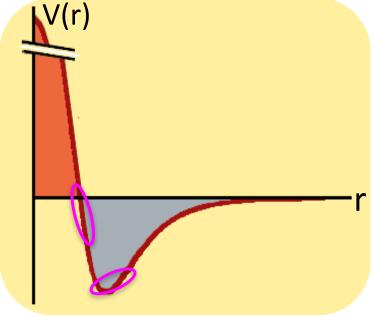






Nuclear Physics

Better understanding of the nucleon interaction and the nuclear momentum distribution

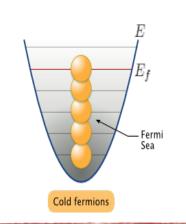


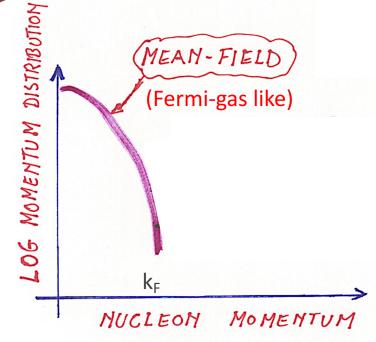




Nuclear Physics

Better understanding of the nucleon-nucleon interaction and the nuclear momentum distribution



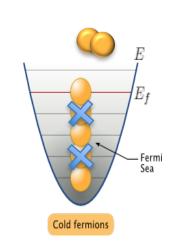


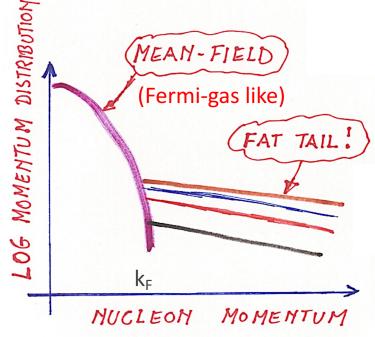




Nuclear Physics

Better understanding of the nucleon-nucleon interaction and the nuclear momentum distribution









You can't do nuclei without correlations!





Today: (short) overview of SRC and a presentation of a new effective theory for SRC in nuclei

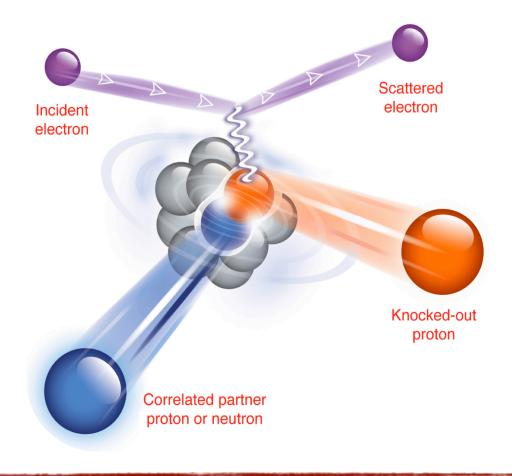
You can't do nuclei without correlations!



Exclusive 2N-SRC Studies



Breakup the pair =>
Detect both nucleons =>
Reconstruct 'initial' state

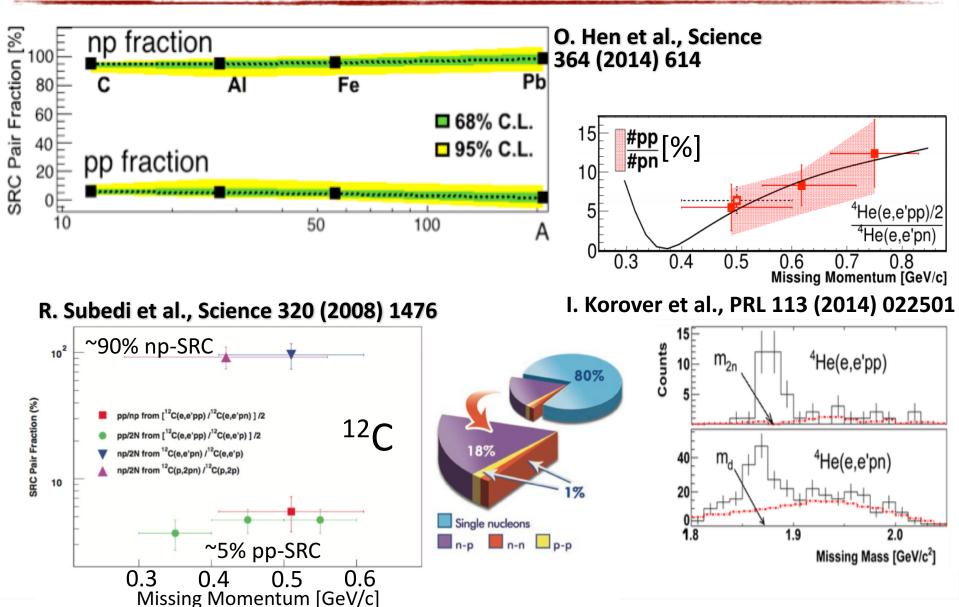






SRC Isospin Structure





A. Tang et al., PRL (2003); E. Piasetzky et al., PRL (2006); R. Shneor et al., PRL (2007)



SRC Isospin Structure

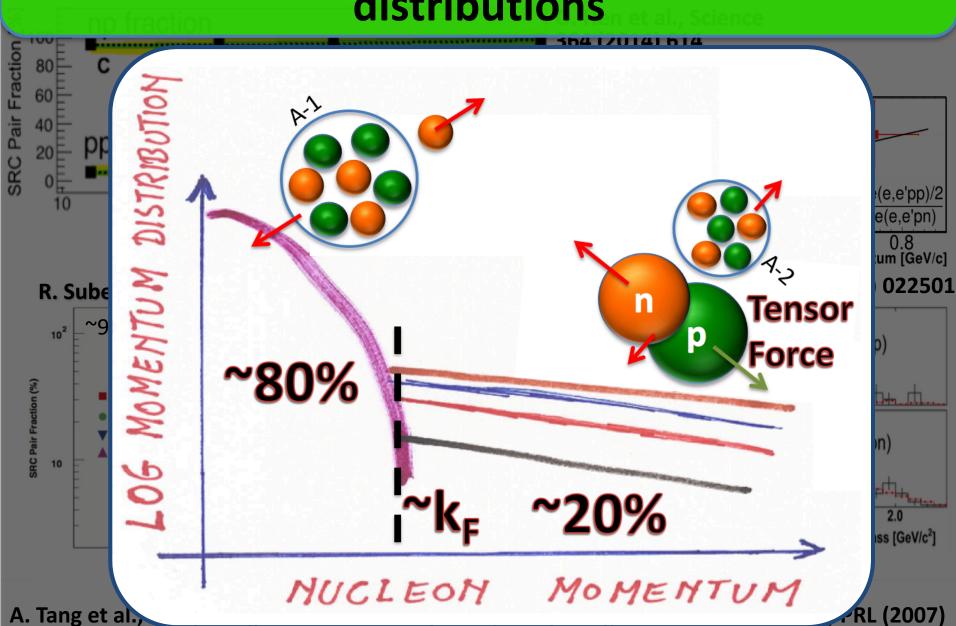


Bottom Line:

- SRCs account for:
 - ~ 20% of the nucleons in nuclei.
 - ~100% of the high-p (k>k_F) nucleons in nuclei.
- Predominantly due to np-SRC.
- Universal for A = 4 208 nuclei.
- <u>Tensor force</u> dominance at short distance.

0.3 0.4 0.5 0.6 Missing Momentum [GeV/c]

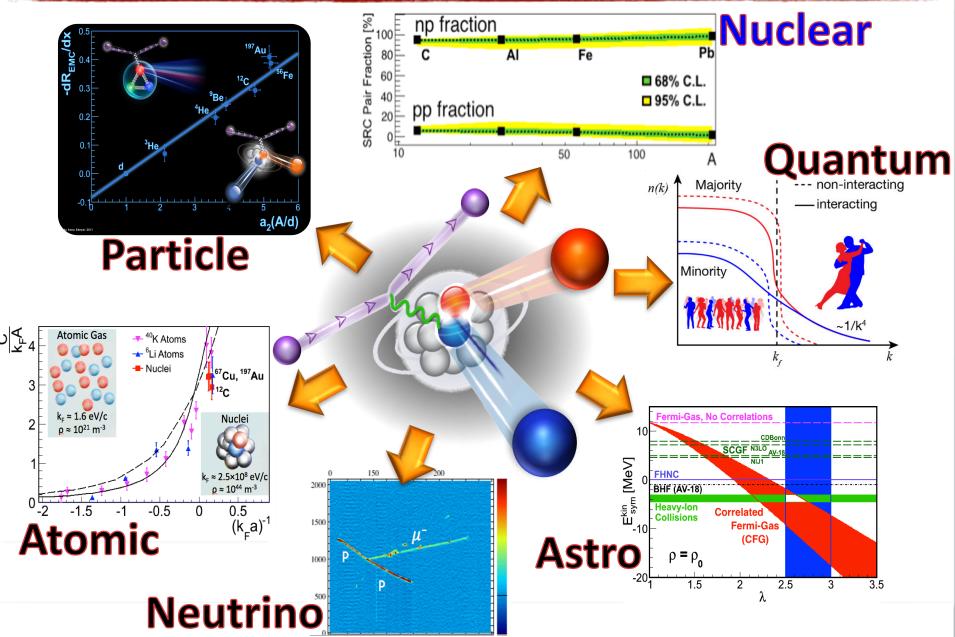
Universal structure of nuclear momentum distributions





Importance of SRC Properties





Two-component interacting Fermi systems

The contact term

Please forget about nuclear physics for a moment







Concept developed for dilute two-component Fermi systems with a short-range (δ -like) interaction.

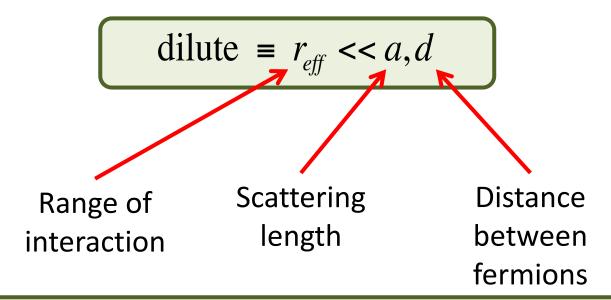
dilute =
$$r_{eff} << a, d$$

Dilute System





Concept developed for dilute two-component Fermi systems with a short-range (δ -like) interaction.



Range of interaction much smaller than the other relevant length scales in the problem

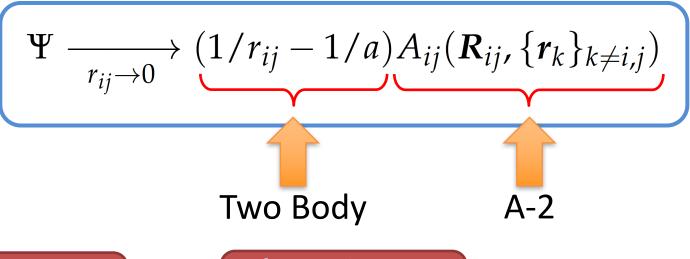
Dilute System





Contact interaction is represented through a boundary condition

Imposing this B.C. on the Schrödinger equation yields an asymptotic wave function when two fermions get very close



Dilute System



Short Distance Factorization





$$\Psi \xrightarrow[r_{ij}\to 0]{} (1/r_{ij}-1/a)A_{ij}(\mathbf{R}_{ij},\{\mathbf{r}_k\}_{k\neq i,j})$$

$$n(k) = C / k^4 \quad \text{for } k > k_F$$

Dilute System



Short Distance Factorization



High Momentum Tail





$$\Psi \xrightarrow{r_{ij} \to 0} (1/r_{ij} - 1/a) A_{ij}(\mathbf{R}_{ij}, \{\mathbf{r}_k\}_{k \neq i,j})$$

$$n(k) = C/k^4 \text{ for } k > k_F$$

Dilute System



Short Distance Factorization



High Momentum Tail





$$\Psi \xrightarrow{r_{ij} \to 0} (1/r_{ij} - 1/a) A_{ij}(\mathbf{R}_{ij}, \{\mathbf{r}_k\}_{k \neq i,j})$$



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Short Distance Factorization



High Momentum Tail





$$\Psi \xrightarrow{r_{ij} \to 0} (1/r_{ij} - 1/a) A_{ij}(\mathbf{R}_{ij}, \{\mathbf{r}_k\}_{k \neq i,j})$$

$$n(k) = C / k^4 \quad \text{for } k > k_F$$

Tan's Contact term:

- 1. Measures the number of SRC different fermion pairs.
- 2. Determines the thermodynamics through a series of universal relations.

Dilute System



Short Distance Factorization



High Momentum Tail

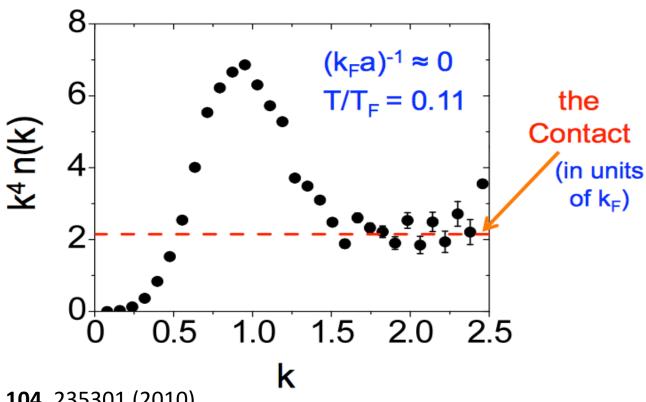


Experimental Validation



Two spin-state mixtures of ultra-cold ⁴⁰K and ⁶Li atomic gas systems.

=> extracted the contact and verified the universal relations







What About a *Nuclear*Contact?





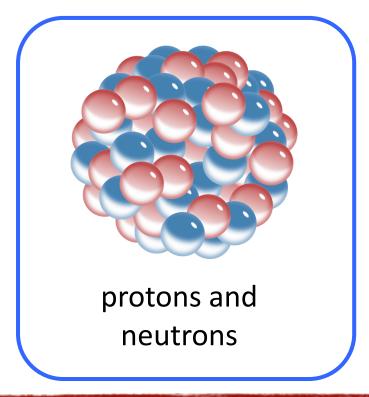
A Nuclear Contact?

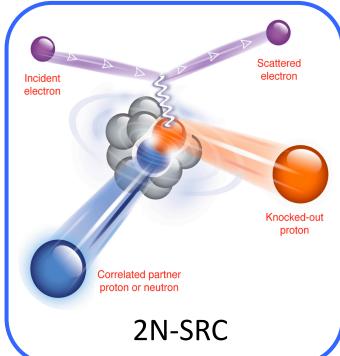


Concept developed for:

dilute two-component Fermi systems with a short-range interaction.









Theory Says: not so much



Are nuclei dilute? (i.e. r_{eff} << a,d)

$$r_{eff} \approx \frac{\hbar}{2 \cdot m_{\pi} \cdot c} \approx 0.7 \text{ fm}$$

[Tensor force]

$$d = \left(\frac{\rho}{2}\right)^{-1/3} \approx 2.3 \text{ fm}$$

$$a(^{3}S_{1}) = 5.42 \text{ fm}$$

 $r_{eff}(0.7 \text{ fm}) < d(2.3 \text{ fm}), a(5.4 \text{ fm})$



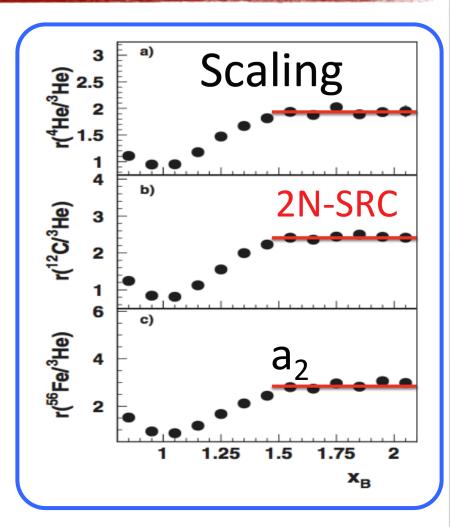
But Experiment Says....



Is there 1/k⁴ scaling regardless?

$$1.5k_F < k < 3k_F$$

$$n_A(k) = a_2(A/d) \cdot n_d(k)$$
 nucleus A deuteron momentum distribution momentum distribution experimental constant



The momentum distribution of nucleons in medium to heavy nuclei is proportional to that of deuteron at high momenta.





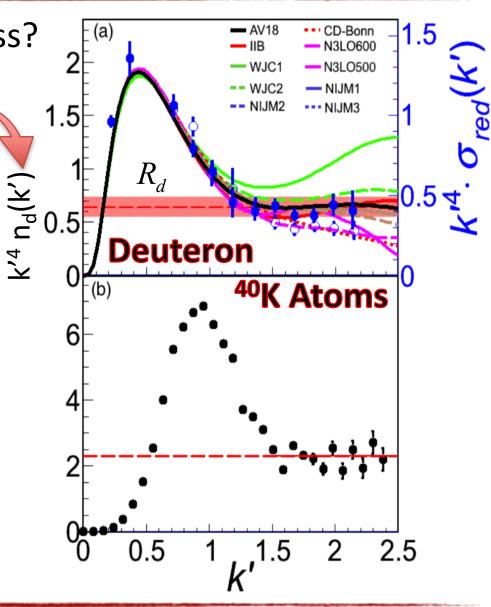
But Experiment Says....



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O. Hen et al. Phys. Rev. C **92**, 045205 (2015)





But Experiment Says.... Yes! (?)



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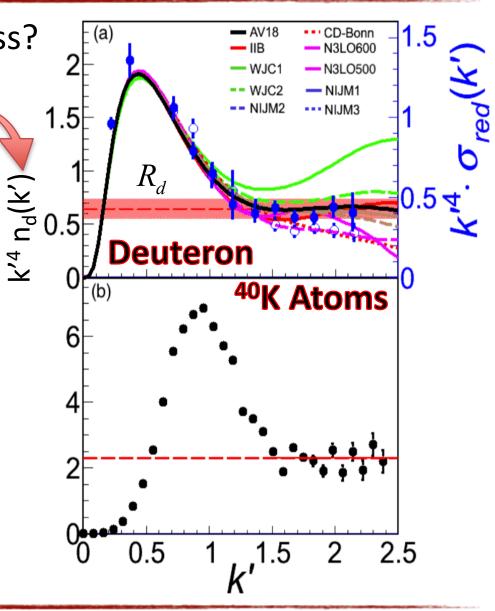
Why 1/k⁴?

Effect of the one pion exchange (OPE) contribution to the tensor potential acting in second order

$$\left(-B-H_{0}\right)\left|\Psi_{D}\right\rangle=V_{T}\left|\Psi_{S}\right\rangle$$

$$V_{00} = V_T \left(-B - H_0 \right)^{-1} V_T$$

O. Hen et al. Phys. Rev. C 92, 045205 (2015)





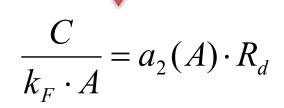
But Experiment Says.... Yes! (?)



Is there 1/k⁴ scaling regardless?

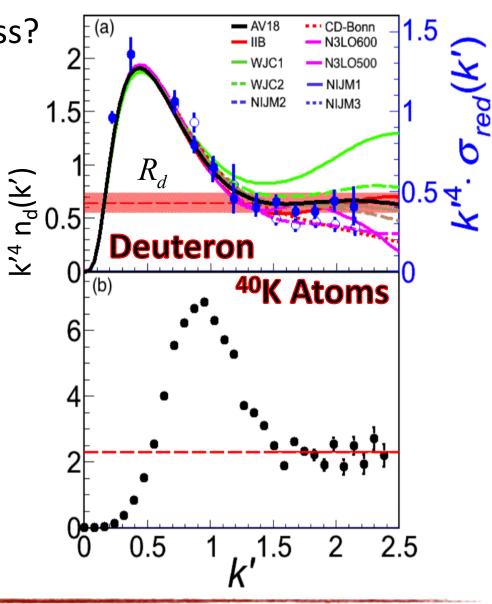
$$1.5k_F < k < 3k_F$$

$$n_A(k) = a_2(A/d) \cdot n_d(k)$$



| Nucleus | - () | $rac{C}{k_F A}$ |
|---------------------|-----------------|------------------|
| | 4.75 ± 0.16 | 3.04 ± 0.49 |
| 56 Fe | 5.21 ± 0.20 | 3.33 ± 0.54 |
| $^{197}\mathrm{Au}$ | 5.16 ± 0.22 | 3.30 ± 0.53 |

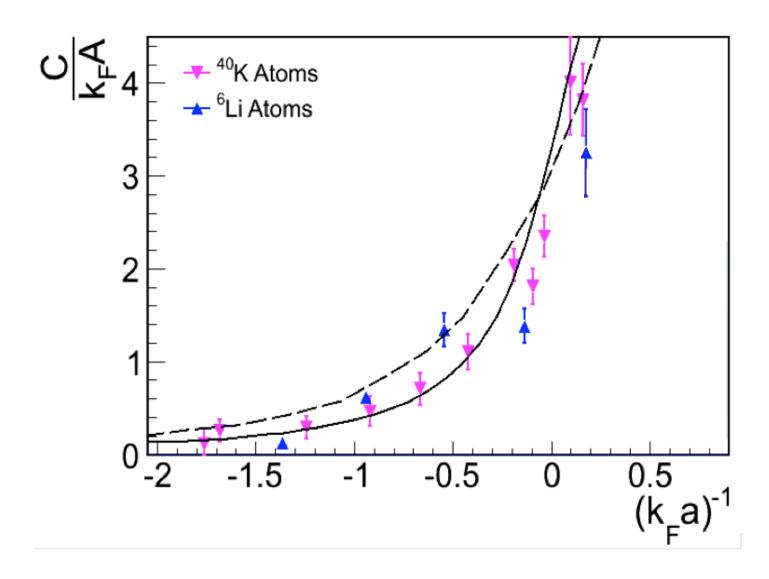
O. Hen et al. Phys. Rev. C **92**, 045205 (2015)





Comparing with atomic systems



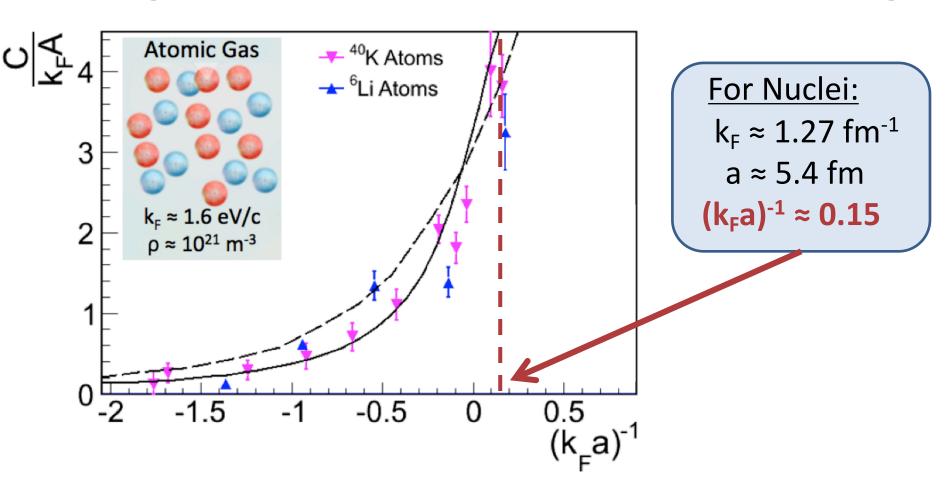




Comparing with atomic systems



Finding the same dimensionless interaction strength



Stewart et al. Phys. Rev. Lett. **104**, 235301 (2010) Kuhnle et al. Phys. Rev. Lett. **105**, 070402 (2010)

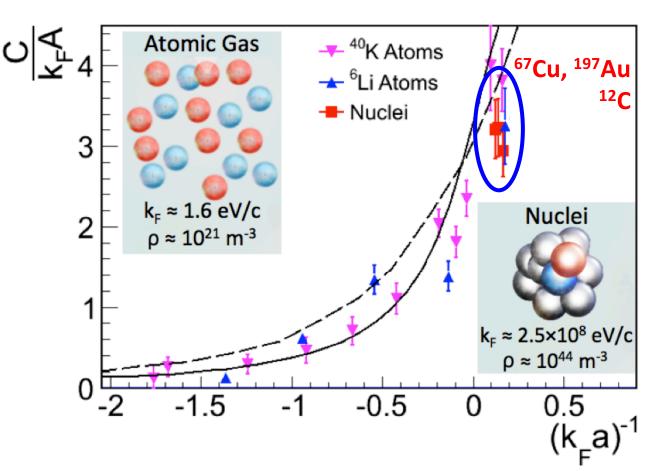




Comparing with atomic systems



Equal contacts for equal interactions strength!



O. Hen et al. Phys. Rev. C **92**, 045205 (2015) Stewart et al. Phys. Rev. Lett. **104**, 235301 (2010) Kuhnle et al. Phys. Rev. Lett. **105**, 070402 (2010)

For Nuclei:

 $k_F \approx 1.27 \text{ fm}^{-1}$ $a \approx 5.4 \text{ fm}$ $(k_F a)^{-1} \approx 0.15$

| Nucleus | $rac{C}{k_F A}$ |
|---------------------|-------------------------|
| $^{12}\mathrm{C}$ | $\boxed{3.04 \pm 0.49}$ |
| 56 Fe | $\boxed{3.33 \pm 0.54}$ |
| $^{197}\mathrm{Au}$ | $\boxed{3.30 \pm 0.53}$ |

$$\frac{C}{k_F \cdot A} = a_2(A) \cdot R_d$$





How can we reconcile the experimental observation with theory expectation?

i.e. is there a region in which the nuclear wave function fully factorizes?









Going Back to the Theory...

- 1. Generalize the contact formalism to nuclear systems.
- 2. Use it to make specific predictions of nuclear properties.
- 3. Check using experimental data and full many-body calculations.





Issue: Scale separation does not necessarily work in nuclear systems.

Solution: assume a more general form for the 2-body wavefunction.

Atomic System:

$$\Psi \xrightarrow[r_{ij}\to 0]{} (1/r_{ij}-1/a)A_{ij}(\mathbf{R}_{ij},\{\mathbf{r}_k\}_{k\neq i,j})$$

Nuclear System:

$$\Psi \xrightarrow[r_{ij} \to 0]{} (\boldsymbol{\varphi(r)_{ij}}) A_{ij}(\boldsymbol{R}_{ij}, \{\boldsymbol{r}_k\}_{k \neq i,j})$$





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Nuclear System:

$$\Psi \xrightarrow[r_{ij} \to 0]{} (\boldsymbol{\varphi(r)_{ij}}) A_{ij}(\boldsymbol{R}_{ij}, \{\boldsymbol{r}_k\}_{k \neq i,j})$$

known solution for the two-body (nuclear) problem



Factorization in Nuclei



Consider the factorized wave function:

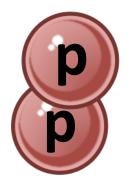
$$\Psi \xrightarrow[r_{ij}\to 0]{} \sum_{\alpha} \varphi_{\alpha}(\mathbf{r}_{ij}) A_{ij}^{\alpha}(\mathbf{R}_{ij}, \{\mathbf{r}_k\}_{k\neq i,j})$$

In nuclear physics we have 3 possible types of pairs:

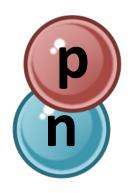


For each pair we have different channels

$$\alpha = (s,l)jm$$











Factorization in Nuclei



Consider the factorized wave function:

$$\Psi \xrightarrow[r_{ij}\to 0]{} \sum_{\alpha} \varphi_{\alpha}(\mathbf{r}_{ij}) A_{ij}^{\alpha}(\mathbf{R}_{ij}, \{\mathbf{r}_k\}_{k\neq i,j})$$

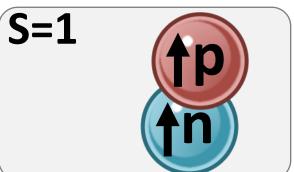
In nuclear physics we have 3 possible types of pairs:



For each pair we have different channels

$$\alpha = (s,l)jm$$

Reduced to 2 contacts by imposing L=0 and symmetry considerations





Relating to Momentum Space



$$\Psi \xrightarrow{r_{ij}\to 0} \sum_{\alpha} \varphi_{\alpha}(\mathbf{r}_{ij}) A_{ij}^{\alpha}(\mathbf{R}_{ij}, \{\mathbf{r}_k\}_{k\neq i,j})$$

One Body:

$$n_p(k) = \sum_{\alpha} \left| \widetilde{\varphi}_{pp}^{\alpha}(k) \right|^2 2C_{pp}^{\alpha} + \sum_{\alpha} \left| \widetilde{\varphi}_{pn}^{\alpha}(k) \right|^2 C_{pn}^{\alpha}$$



2-Body momentum distributions



One Body momentum distribution [n_N(k)]:
 Probability to find a nucleon, N, in the nucleus with momentum k.

Two Body momentum distribution [n_{NN}(q,Q)]:
 Probability to find a NN pair in the nucleus with relative (c.m.) momentum q (Q).

 $n_{NN}(q,Q)$ – computational Frontier!



Momentum Space Factorization



$$\Psi \xrightarrow[r_{ij}\to 0]{} \sum_{\alpha} \varphi_{\alpha}(\mathbf{r}_{ij}) A_{ij}^{\alpha}(\mathbf{R}_{ij}, \{\mathbf{r}_k\}_{k\neq i,j})$$

One Body:

$$n_p(k) = \sum_{\alpha} \left| \widetilde{\varphi}_{pp}^{\alpha}(k) \right|^2 2C_{pp}^{\alpha} + \sum_{\alpha} \left| \widetilde{\varphi}_{pn}^{\alpha}(k) \right|^2 C_{pn}^{\alpha}$$

Two body:

$$F_{ij}(k) = \sum_{\alpha} \left| \widetilde{\varphi}_{ij}^{\alpha}(k) \right|^2 C_{ij}^{\alpha}$$

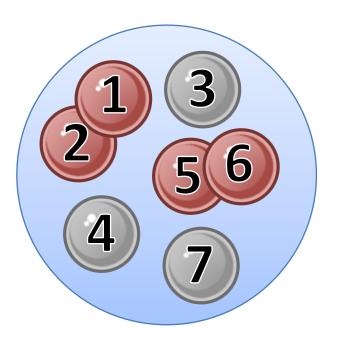
$$n_p(k) \xrightarrow[k\to\infty]{} 2F_{pp}(k) + F_{pn}(k)$$



Two-Body Momentum Distributions



 $n_{NN}(q,Q)$ – Mathematical object that counts all possible NN pairs, regardless of their state:



Consider all NN pairs:

1-2 2-3 3-4 4-5 **5-6** 6-7

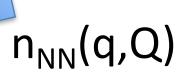
1-3 2-4 3-5 4-6 5-7

1-4 **2-5** 3-6 4-7

1-5 2-6 3-7

1-6 2-7

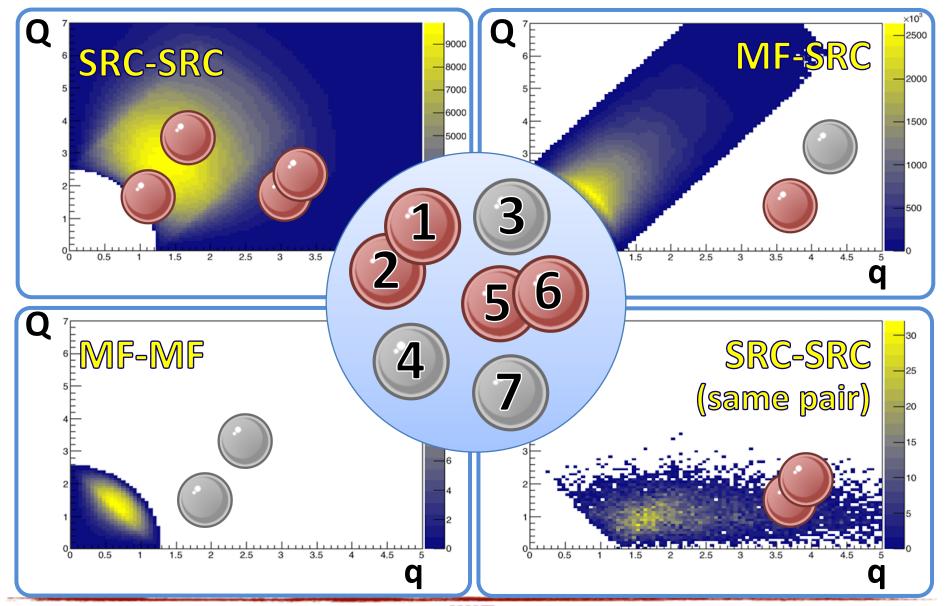
1-7





Toy model to the rescue

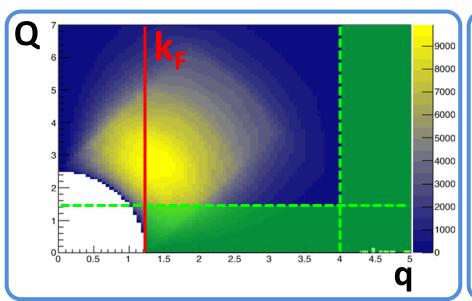


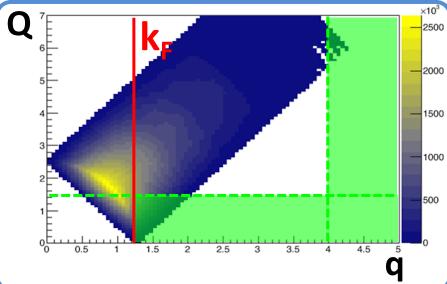


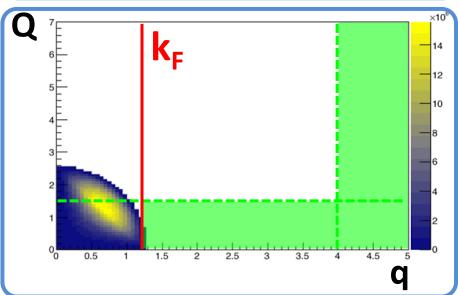


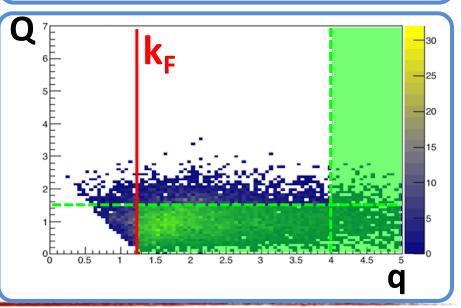
Toy model to the rescue









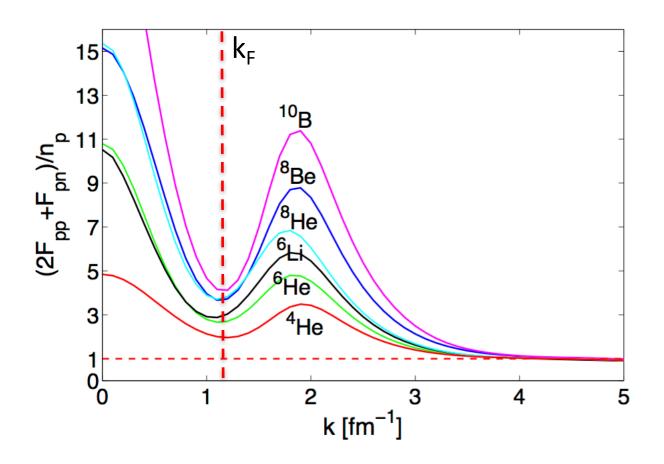




Two-Body Scaling for High q



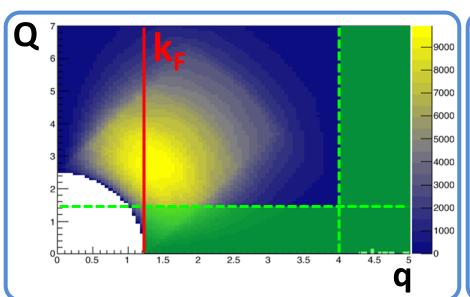
• Weiss and Barnea (PRC 2015): contact interactions dominate when $n_{pn}(q)+2n_{pp}(q)=n_{p}(k)$

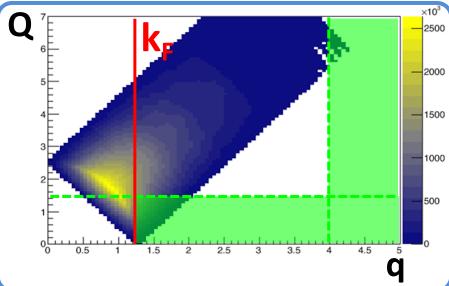


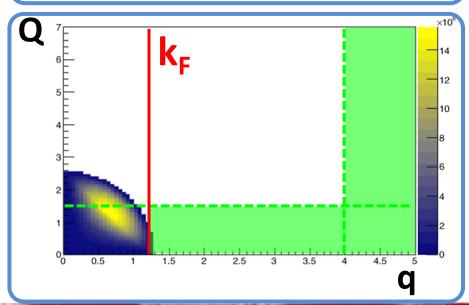


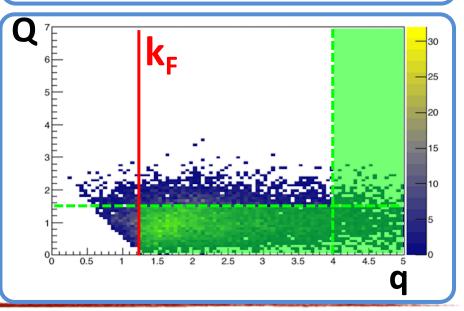
Toy model to the rescue









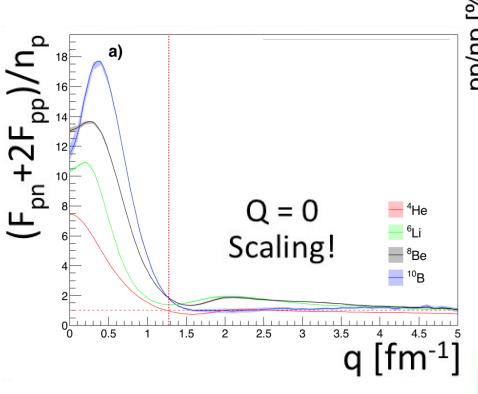


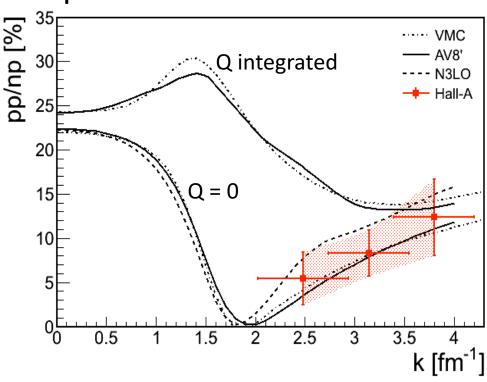


Two-Body Scaling for **Q=0**



 Restricting Q=0 restores scaling starting from k>k_F AND gives consistent results with experimental data!





SRC pairs are consistent with Q = 0 back-to-back pairs

R. Wiringa et al., Phys. Rev. C 89, 024305 (2014).

T. Neff, H. Feldmeier and W. Horiuchi, Phys. Rev. C 92, 024003 (2015).

I. Korover, N. Muangma, and O. Hen et al., Phys. Rev. Lett 113, 022501 (2014).

Weiss, Cruz-Torres, Barnea, Piasetzky and Hen, arXiv 1612.00923 (2016)



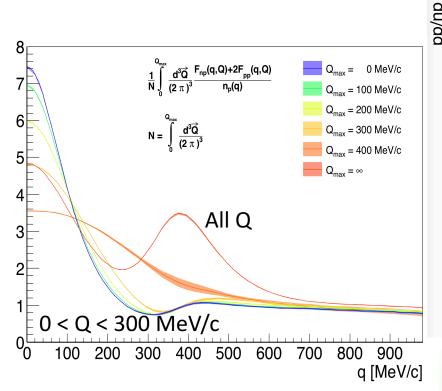


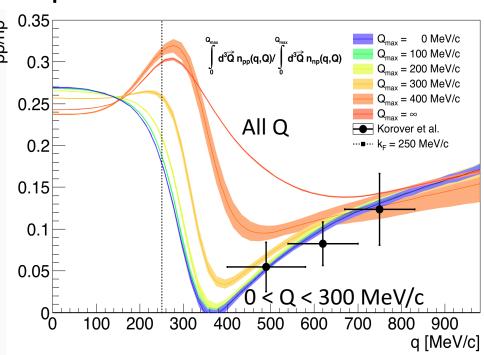
 $(F_{np} + 2F_{pp})/n$

Two-Body Scaling for Low Q



 Restricting Q=0 restores scaling starting from k>k_F AND gives consistent results with experimental data!





SRC pairs are consistent with $Q \le k_F back-to-back$ pairs

R. Wiringa et al., Phys. Rev. C 89, 024305 (2014).

T. Neff, H. Feldmeier and W. Horiuchi, Phys. Rev. C 92, 024003 (2015).

I. Korover, N. Muangma, and O. Hen et al., Phys. Rev. Lett 113, 022501 (2014).

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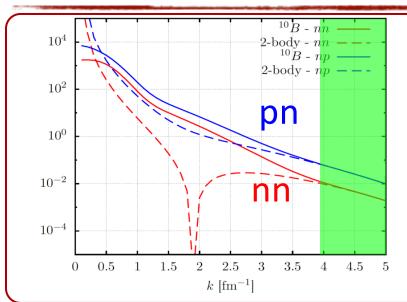
Extracting the nuclear contact(s)





Extracting the Contacts



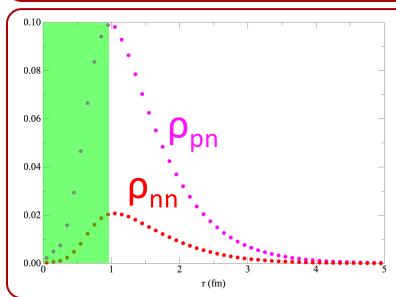


2-Body momentum distributions

$$F_{pn}(k) \underset{k \rightarrow \infty}{\longrightarrow} \left|\phi_{pn}^{0}(k)\right|^{2} \textcolor{red}{C_{pn}^{0}} + \left|\phi_{pn}^{d}(k)\right|^{2} \textcolor{red}{C_{pn}^{d}}$$

$$F_{nn}(k) \xrightarrow[k \to \infty]{} \left|\phi_{nn}^0(k)\right|^2 C_{nn}^0$$

Fitting range ~ 4-5 fm⁻¹



2-Body density distributions

$$\rho_{pn}(r) \mathop{\longrightarrow}\limits_{r \to 0} \left|\phi_{pn}^{0}(r)\right|^{2} \textcolor{red}{C_{pn}^{0}} + \left|\phi_{pn}^{d}(r)\right|^{2} \textcolor{red}{C_{pn}^{d}}$$

$$\rho_{nn}(r) \underset{r \rightarrow 0}{\longrightarrow} \left|\phi_{nn}^{0}(r)\right|^{2} C_{nn}^{0}$$

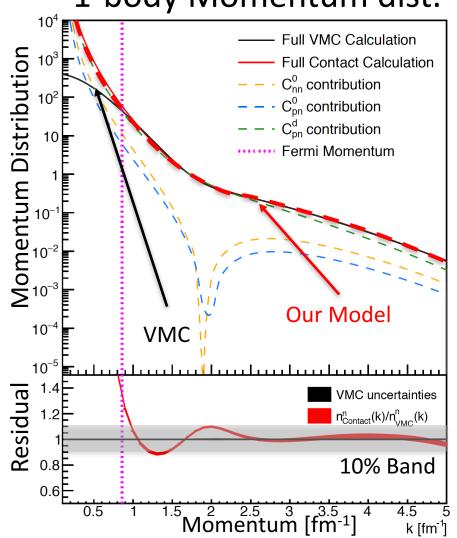
Fitting range ~ 0.25-1 fm



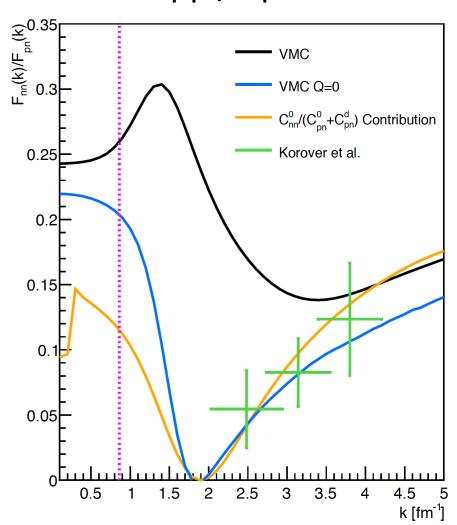
⁴He Results







pp / np ratio



Weiss, Cruz-Torres, Barnea, Piasetzky and Hen, arXiv 1612.00923 (2016)

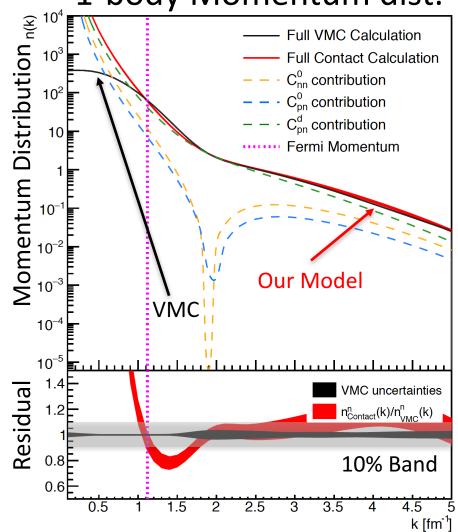




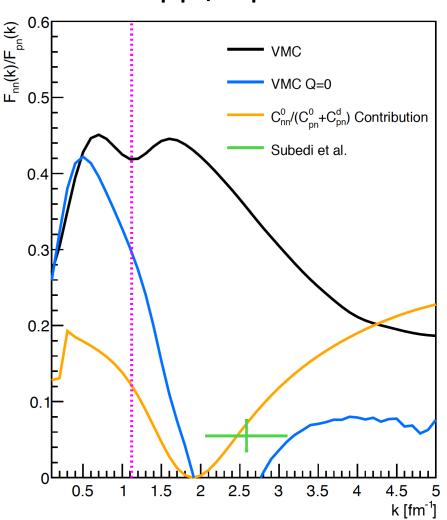
¹²C Results







pp / np ratio



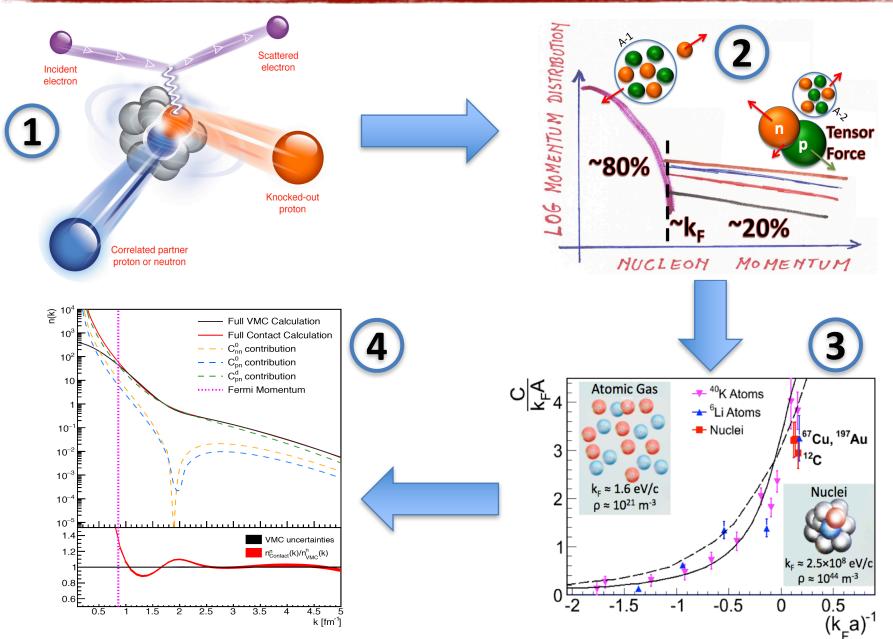
Weiss, Cruz-Torres, Barnea, Piasetzky and Hen, arXiv 1612.00923 (2016)





Summery: Exp. to Pheno. to Theory

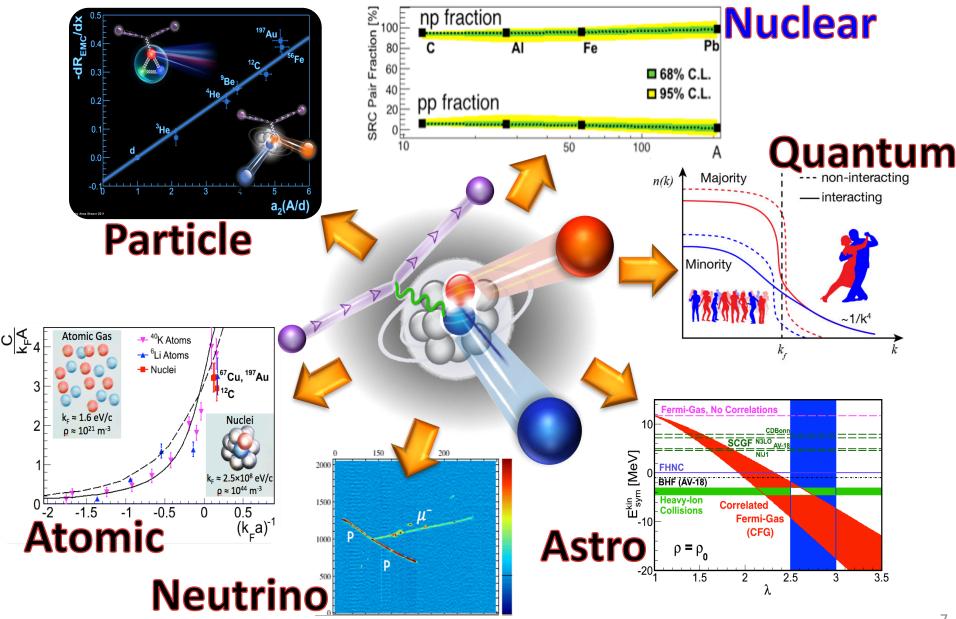






Why SRC?

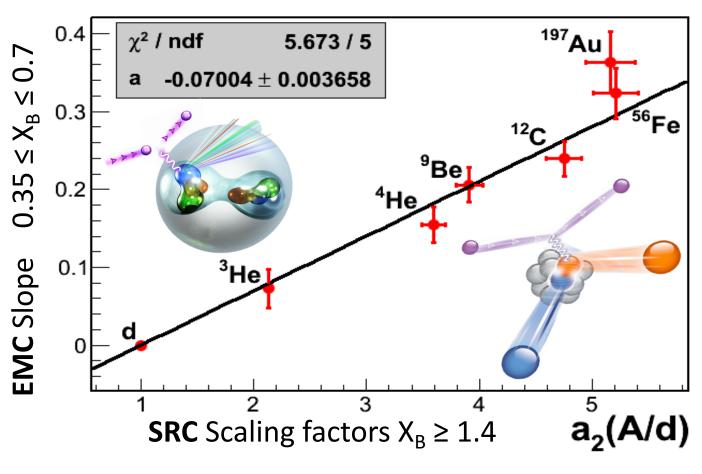




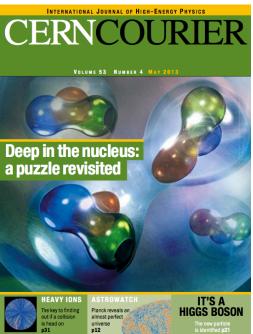


EMC-SRC Correlation





See G. Miller talk yesterday



- O. Hen et al., Int. J. Mod. Phys. E. **22**, 1330017 (2013).
- O. Hen et al., Phys. Rev. C **85** (2012) 047301.
- L. B. Weinstein, E. Piasetzky, D. W. Higinbotham, J. Gomez, O. Hen, R. Shneor, Phys. Rev. Lett. 106 (2011) 052301.





Forthcoming RMP Review



Nucleon-Nucleon Correlations and the Quarks Within

Or Hen

Massachusetts Institute of Technology, Cambridge, MA 02139

Gerald A. Miller

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(Dated: November 2, 2016)

- conventional (non-quark) nuclear physics cannot account for the EMC effect
- models need to include nucleon modification to account for the EMC effect. These models can modify the structure of either:
 - mean field nucleons, or
 - nucleons belonging to SRC pairs.
- there is a phenomenological connection between the strength of the EMC effect and the probability that a nucleon belongs to a two-nucleon SRC pair $(a_2(A))$, see Fig. 33.
- the influence of SRC pairs can account for the EMC-SRC correlation because both effects are driven by high virtuality nucleons with $p^2 \neq M^2$,
- the connection between the EMC effect and the coefficients $a_2(A)$ has been derived using two completely different theories, so that this connection is no accident
- nuclei must contain a small percentage of baryons that are not nucleons. Such baryons exist in the short-ranged correlations and are the source of the EMC effect.

Earthcoming PNAD Pavious

Short Range Correlations and the EMC Effect in Effective Field Theory

Jiunn-Wei Chen, 1, 2, * William Detmold, 2, † Joel E. Lynn, 3, 4, ‡ and Achim Schwenk 3, 4, 5, §

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Gerald A. Miller

the structure of either

d nucleons, or

arXiv: 1607.03065 (2016)

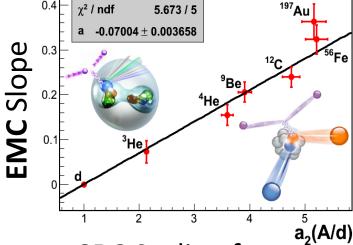
EFT description of bound nucleon structure:

$$F_2^A(x,Q^2)/A = F_2^N(x,Q^2) + g_2(A,\Lambda)f_2(x,Q^2,\Lambda)$$

$$g_2(A,\Lambda) = \underbrace{\frac{1}{A} \langle A | \left(N^\dagger N \right)^2 | A \rangle_{\Lambda}}_{\Lambda}$$

The contact...

$$a_2(A,x>1) = \frac{g_2(A,\Lambda)}{g_2(2,\Lambda)}$$
 [SRC Scaling Factor] $g_2(2,\Lambda)$



SRC Scaling factors



Tagged Structure Functions (JLab12)

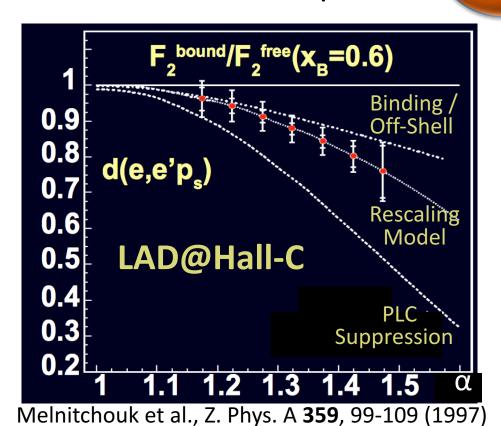


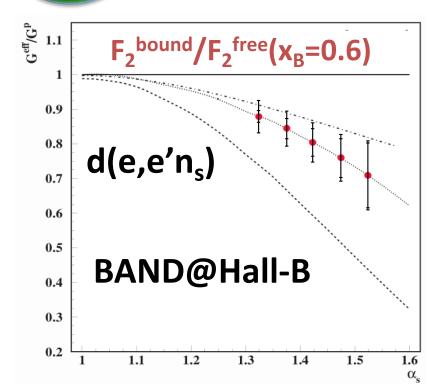
Internal structure of SRC nucleons?

Focus on the deuteron:

(2) Infer its momentum from the recoil partner.

(1) Perform DIS off forward going nucleon.

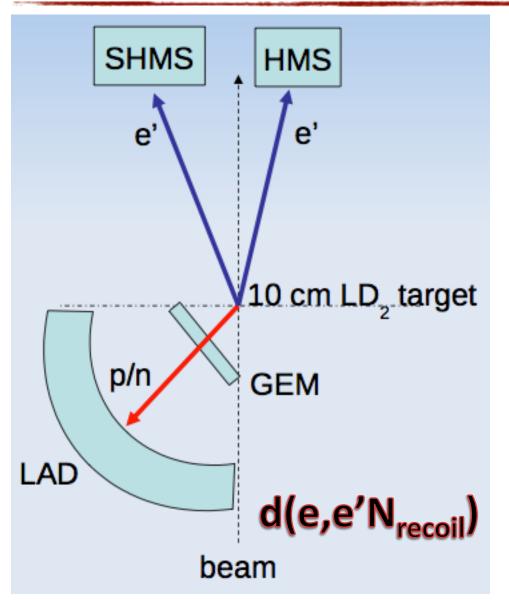






Fixed Target Concept...





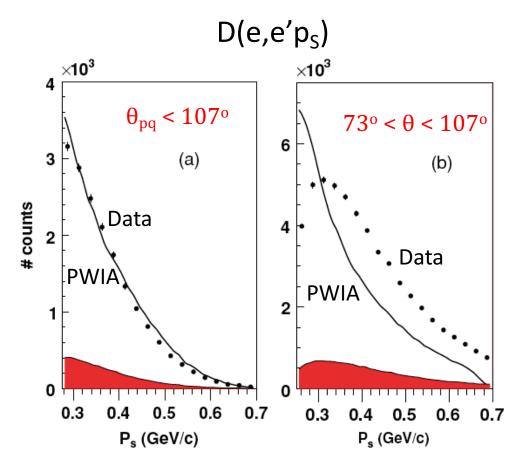
- High resolution spectrometers for d(e,e') measurement in DIS kinematics
- Large acceptance recoil proton \ neutron detector
- Long target + GEM detector – reduce random coincidence



Backward Kinematics:



Minimize Re-Scattering



A. V. Klimenko et al., PRC 73, 035212 (2006)

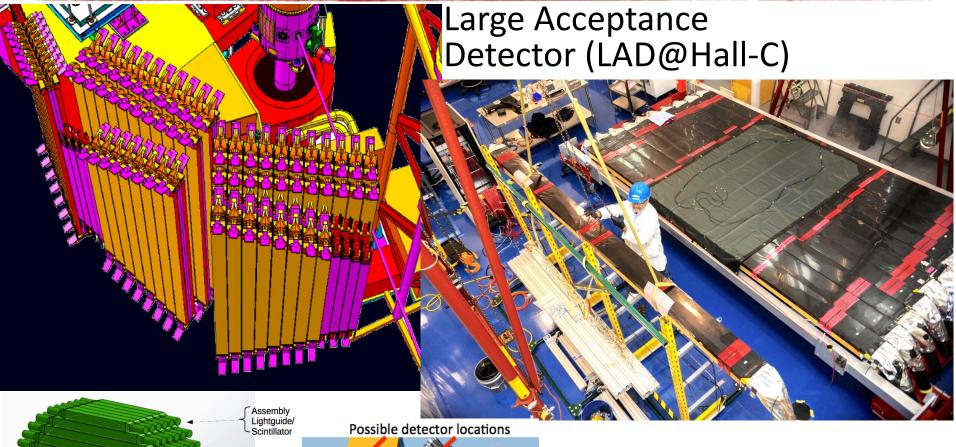
FSI:

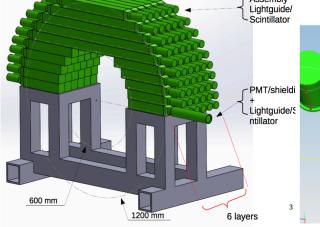
- \triangleright Decrease with Q^2
- ➤ Increase with *W*′
- \triangleright Not sensitive to x'
- \triangleright Small for $\theta_{pq} > 107^{\circ}$



Next Generation Experiments







Backward Angle Neutron Detector (BAND@Hall-B)

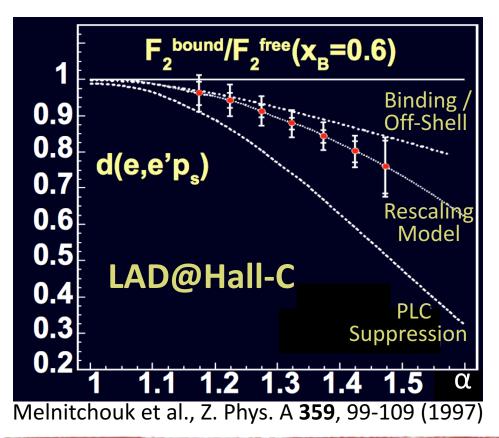
R&D @ MIT /
Construction @ BATES



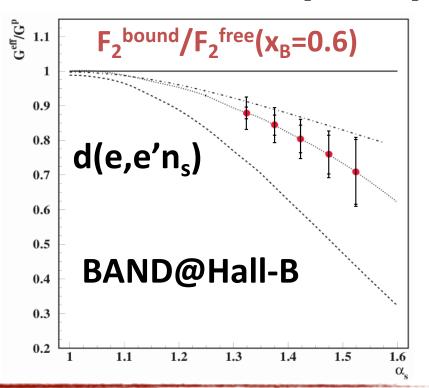
Kinematics and Uncertainties



- Tagging allows to extract the structure function in the nucleon reference frame: $x' = \frac{Q^2}{2(\overline{q} \cdot \overline{p})}$
- Expected coverage: x'~0.3 & 0.45(0.5) < x' < 0.55(0.7) @



 $W^2 > 4 [GeV/c]^2$





The Correlations group







Barak Schmookler



Reynier Torres



Efrain Segarra



Afroditi Papadopoulou



Axel Schmidt



George Laskaris



Maria Patsyuk



Taofeng Wang (*visiting scientist)

TAU (Eli Piasetzky):



Erez Cohen



Meytal Duer



Igor Korover



Adi Ashkenazy





Mariana Khachatryan

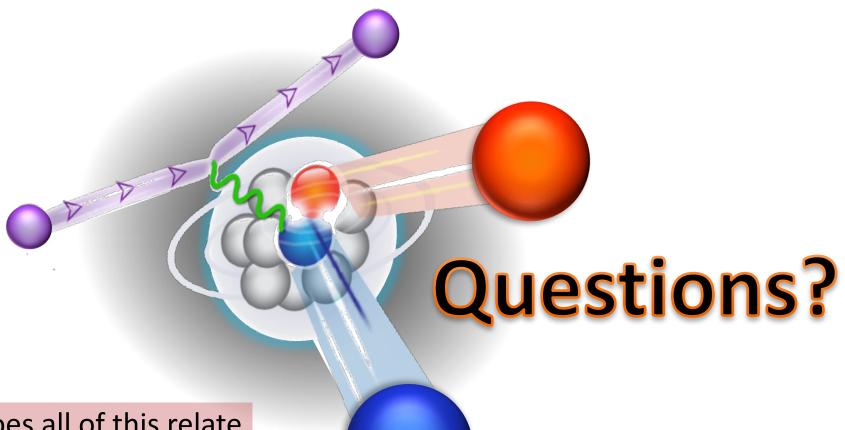


Florian Hauenstein

Theory Collaborators (lots!)

Thank You!





How does all of this relate to the EIC? See G. Miller talk yesterday / W. Cosyn talk tomorrow.